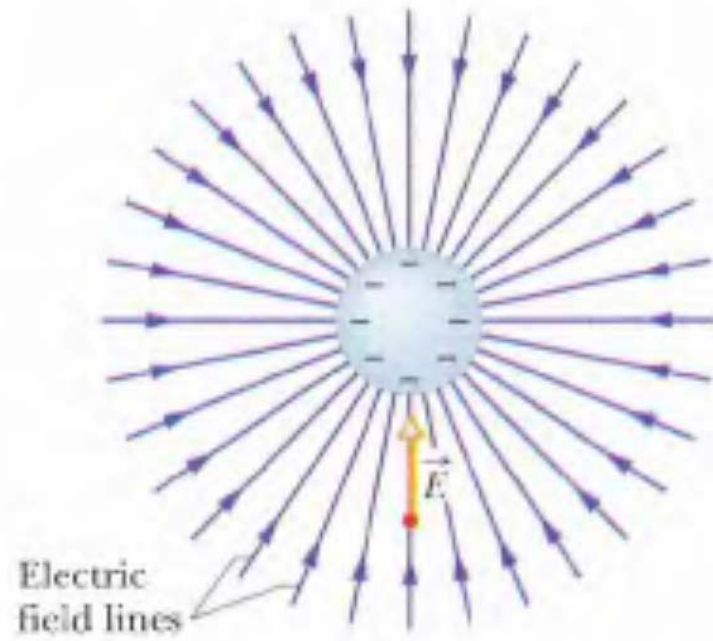
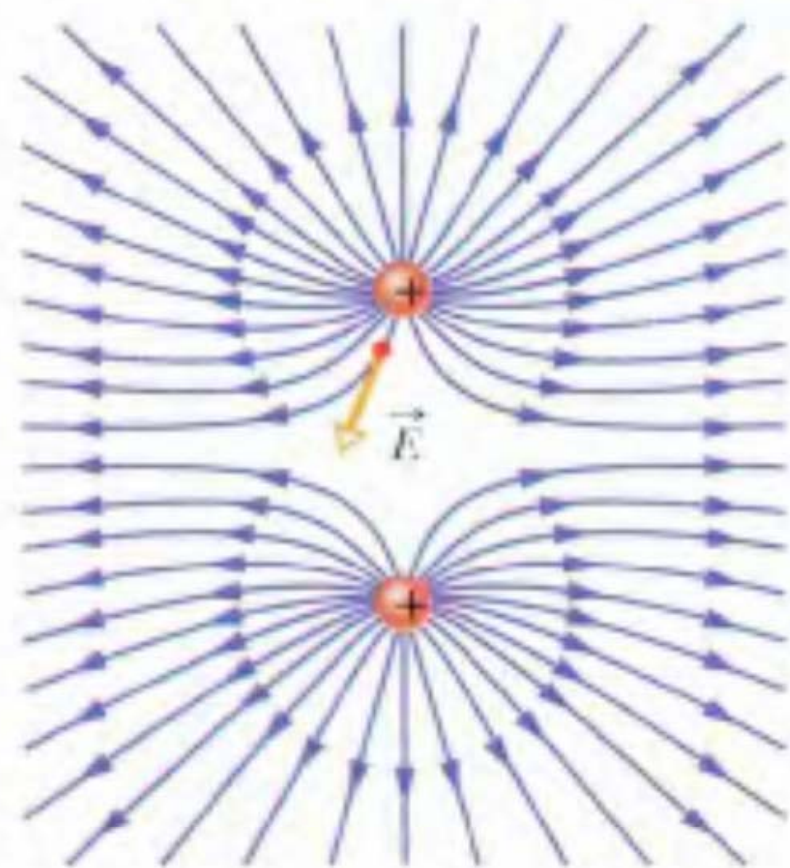


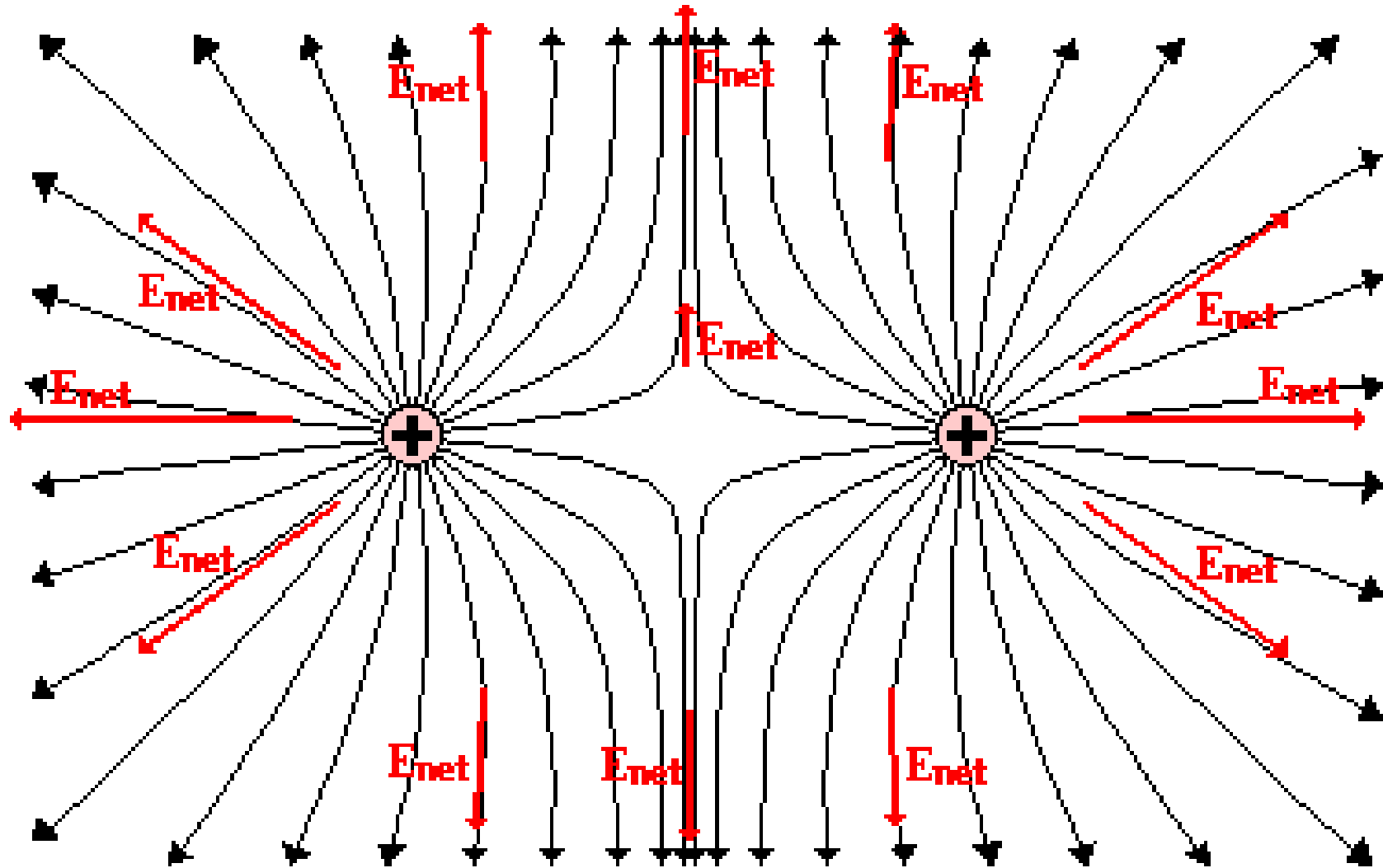
$$\vec{E} = \frac{\vec{F}}{q_0} \quad (\text{electric field}).$$

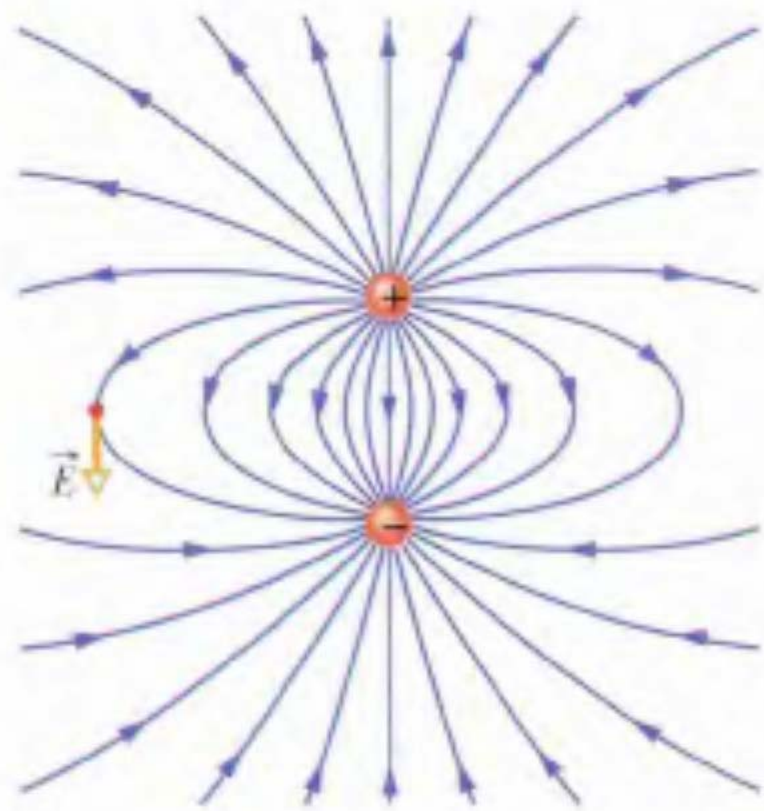
(a)



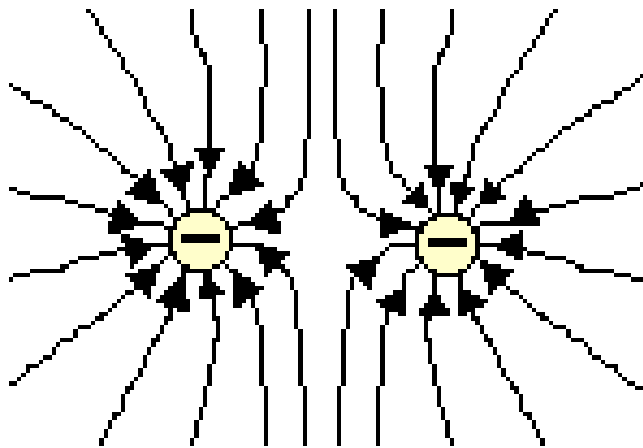
(b)



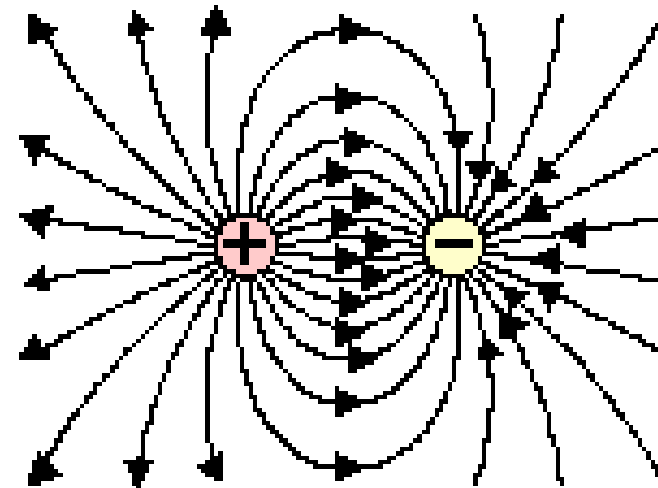




## Other Charge Configurations

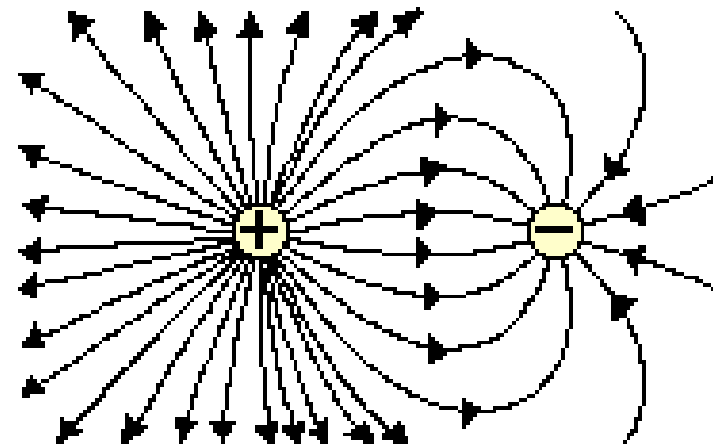
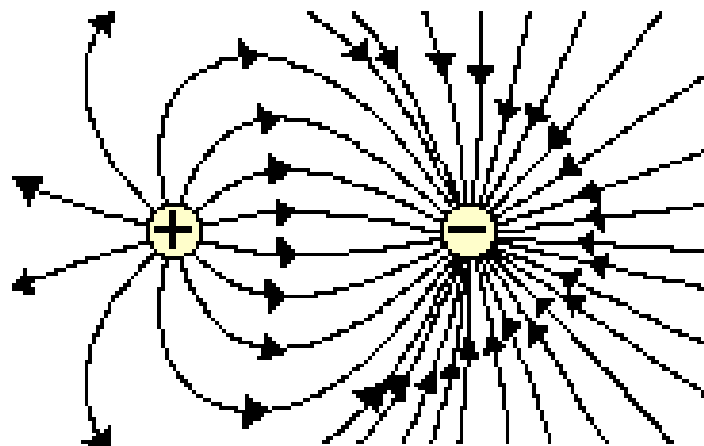
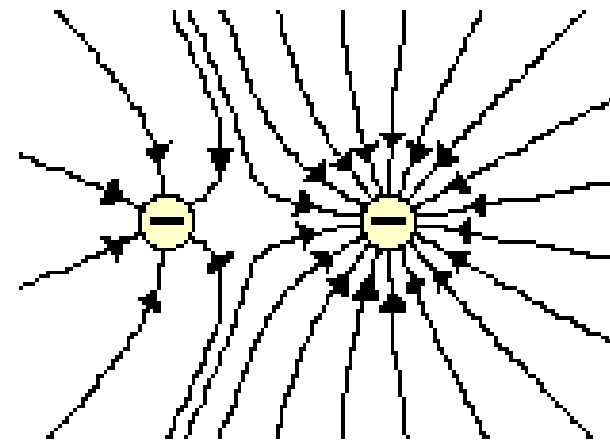
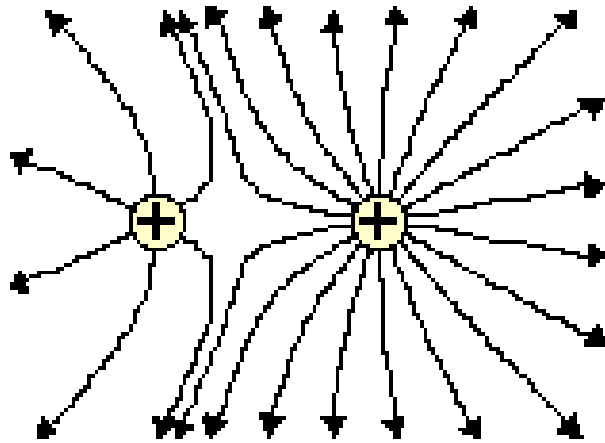


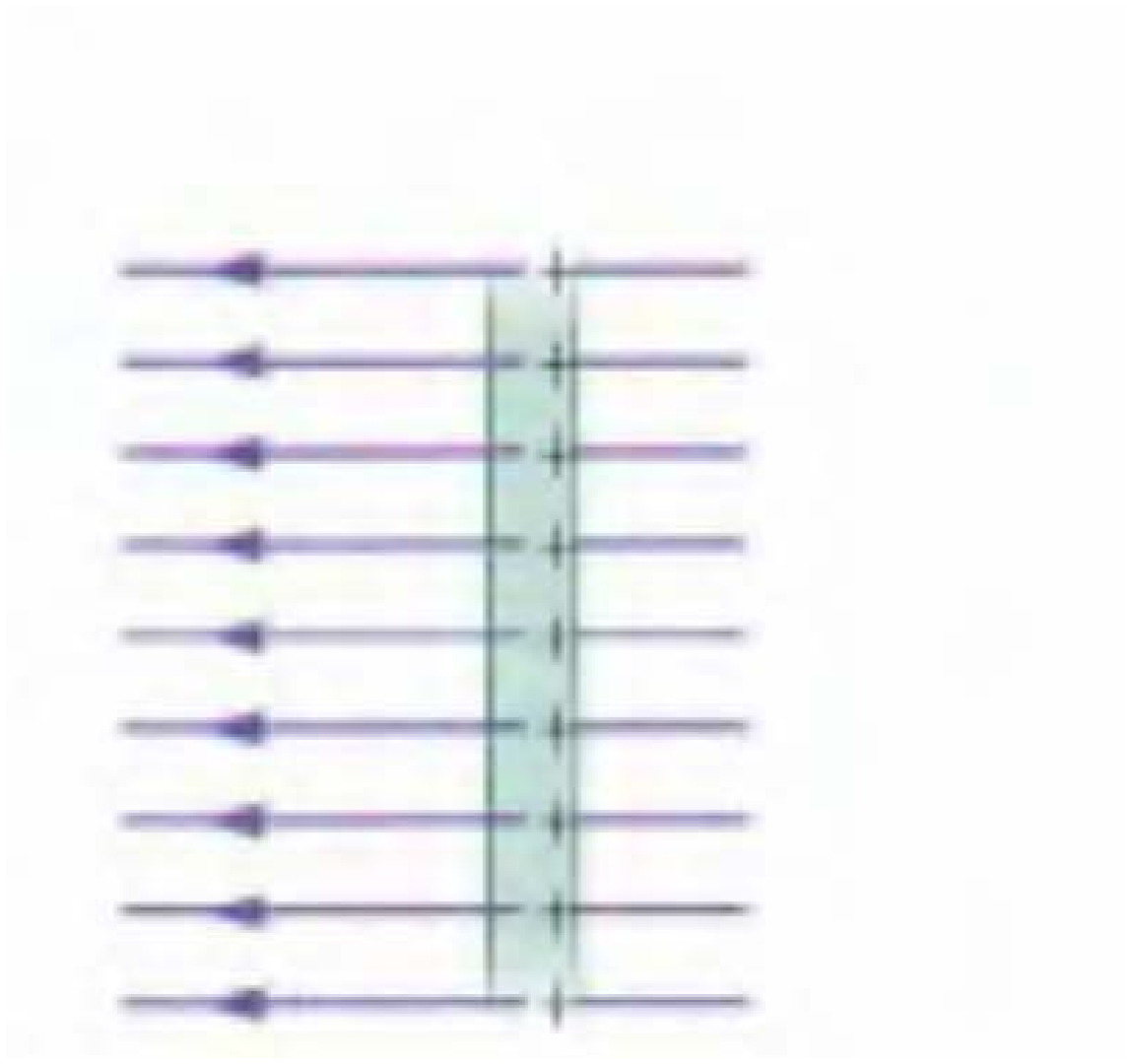
Two Negatively Charged Objects



A Positively and a Negatively Charged Object

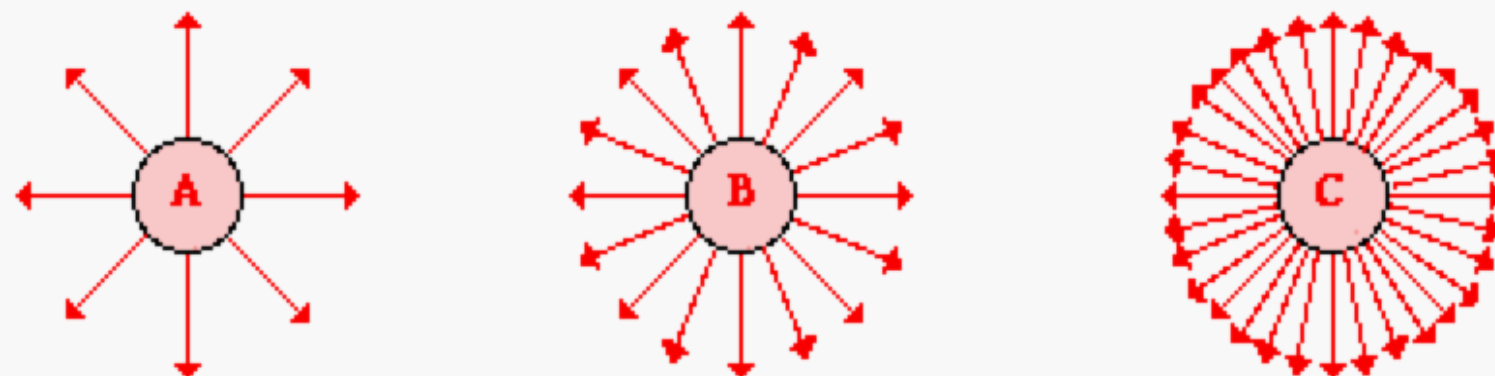
## Electric Field Line Patterns for Objects with Unequal Amounts of Charge



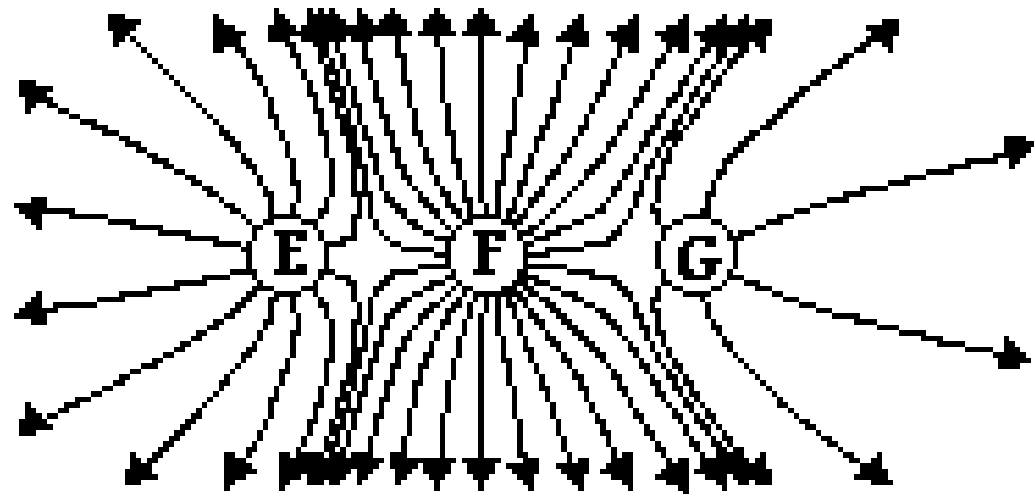


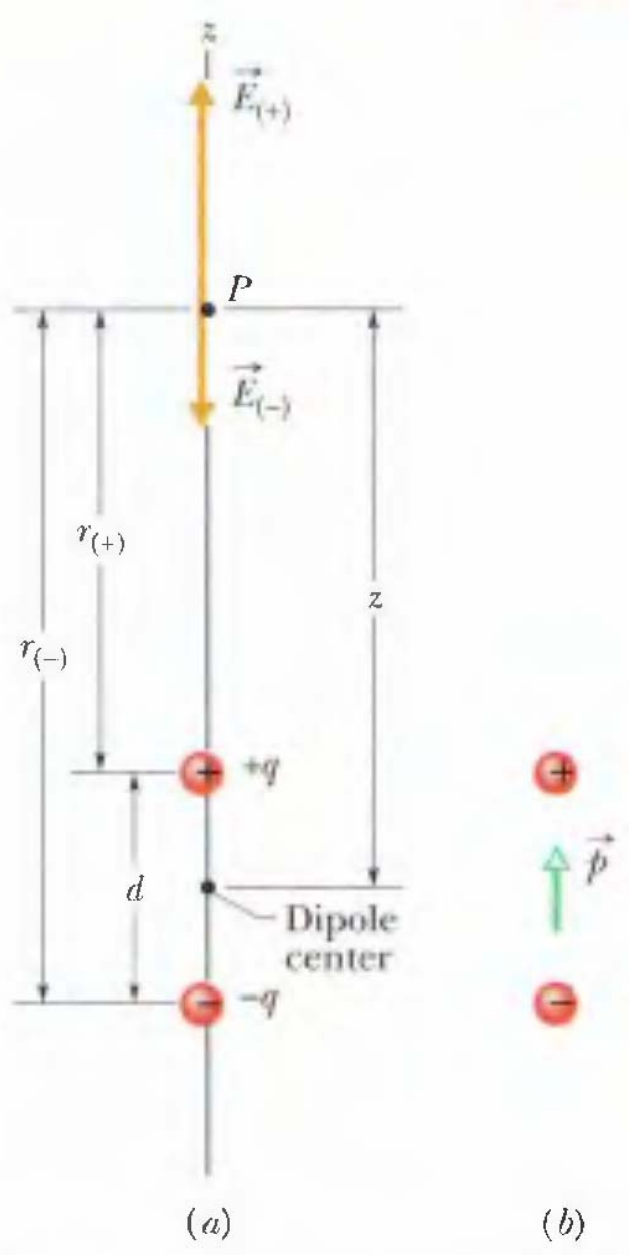


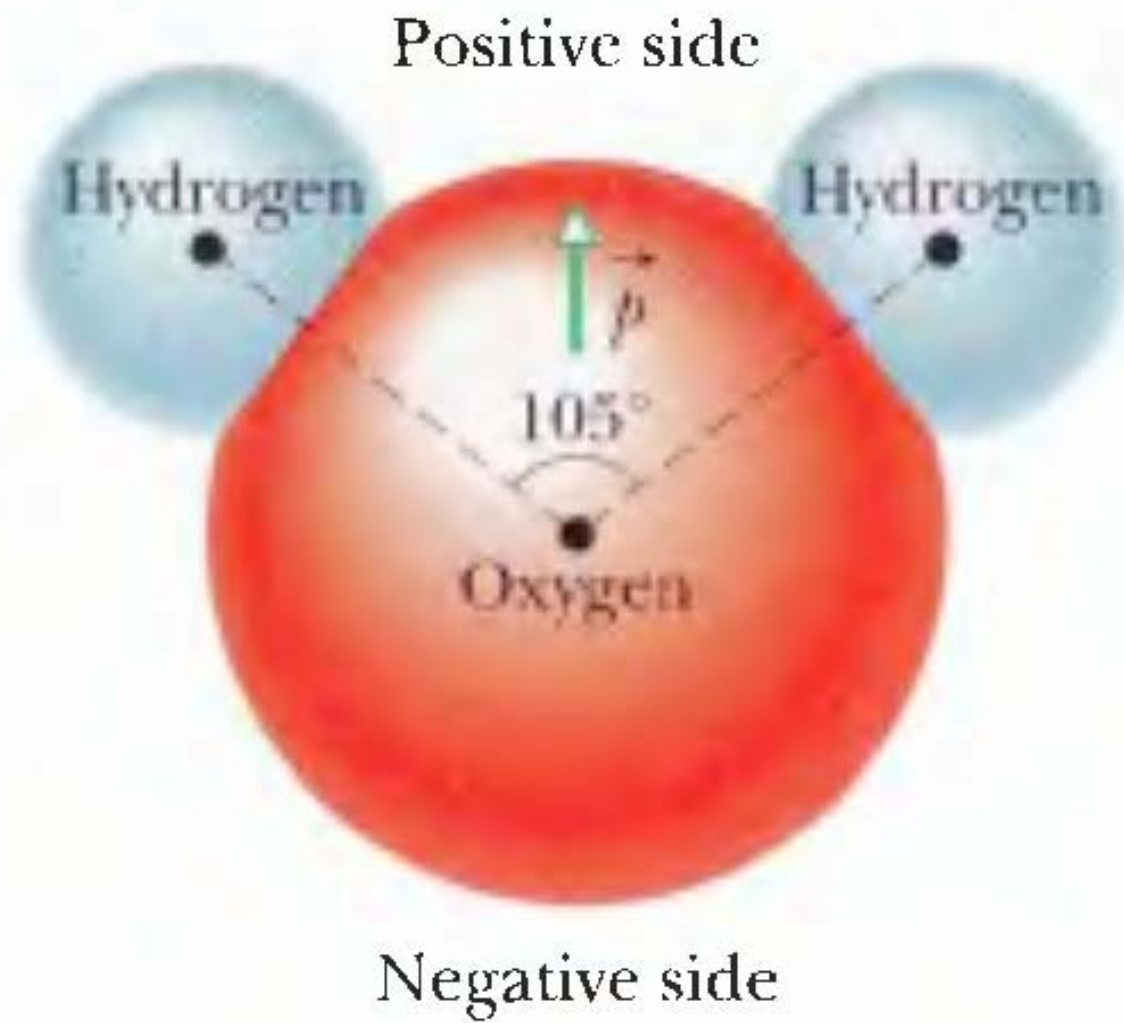
## Density of Lines in Patterns

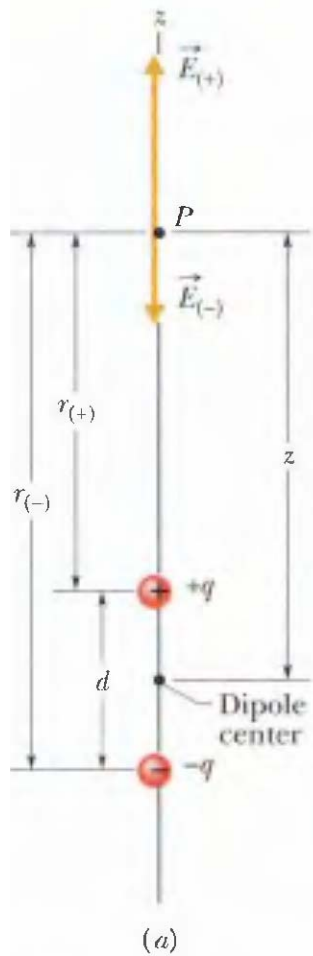


The density of electric field lines around these three objects reveals that the quantity of charge on C is greater than that on B which is greater than that on A.









$$\begin{aligned}
 E &= E_{(+)} - E_{(-)} \\
 &= \frac{1}{4\pi\epsilon_0} \frac{q}{r_{(+)}^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{r_{(-)}^2} \\
 &= \frac{q}{4\pi\epsilon_0(z - \frac{1}{2}d)^2} - \frac{q}{4\pi\epsilon_0(z + \frac{1}{2}d)^2}
 \end{aligned}$$

After some algebra, we can rewrite this equation as

$$E = \frac{q}{4\pi\epsilon_0 z^2} \left( \frac{1}{\left(1 - \frac{d}{2z}\right)^2} - \frac{1}{\left(1 + \frac{d}{2z}\right)^2} \right)$$

By finding a common denominator and multiplying its terms, we come

$$E = \frac{q}{4\pi\epsilon_0 z^2} \frac{2d/z}{\left(1 - \left(\frac{d}{2z}\right)^2\right)^2} = \frac{q}{2\pi\epsilon_0 z^3} \frac{d}{\left(1 - \left(\frac{d}{2z}\right)^2\right)^2}$$

We are usually interested in the electrical effect of a dipole only at distances large compared with the dimensions of the dipole—that is, at distances  $d$ . At such large distances, we have  $d/2z \ll 1$  in Eq. 22-7. Thus, in approximation, we can neglect the  $d/2z$  term in the denominator, which leaves

$$E = \frac{1}{2\pi\epsilon_0} \frac{qd}{z^3}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{p}{z^3} \quad (\text{electric dipole}).$$



## Some Measures of Electric Charge

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Name	Symbol	SI Unit
Charge	$q$	C
Linear charge density	$\lambda$	C/m
Surface charge density	$\sigma$	C/m <sup>2</sup>
Volume charge density	$\rho$	C/m <sup>3</sup>

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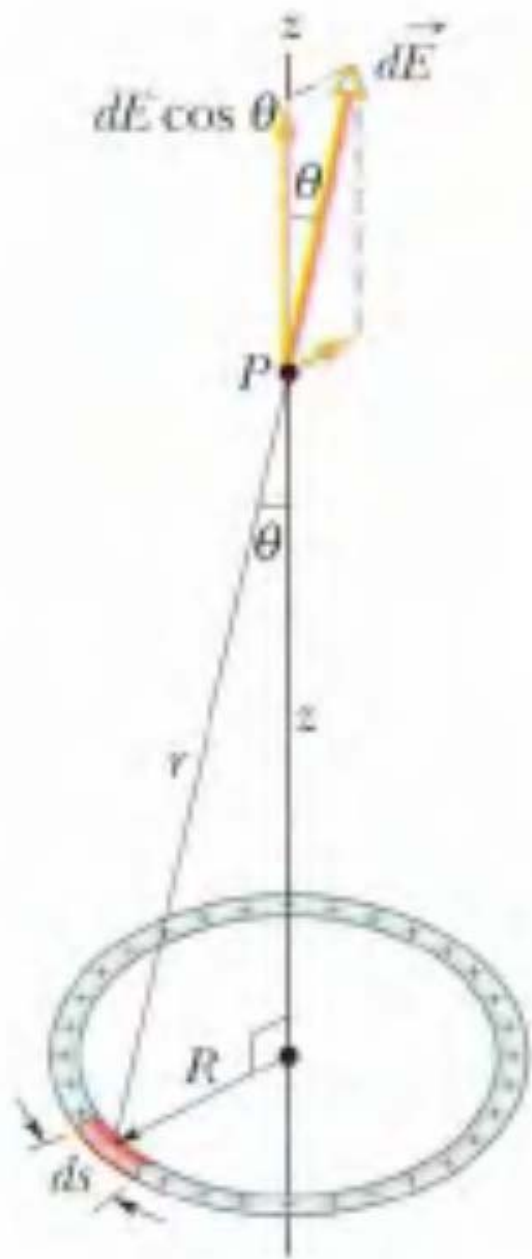




$$dq = \lambda ds.$$

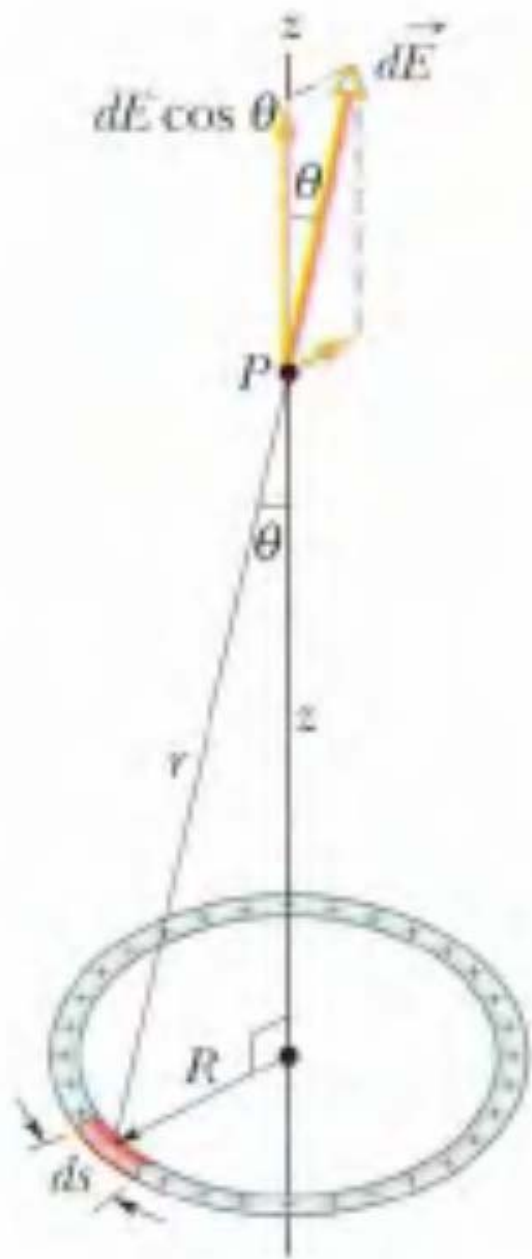
$$dE = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{r^2}.$$

$$dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{(z^2 + R^2)}.$$



$$\cos \theta = \frac{z}{r} = \frac{z}{(z^2 + R^2)^{1/2}}.$$

$$dE \cos \theta = \frac{z \lambda}{4 \pi \epsilon_0 (z^2 + R^2)^{3/2}} ds.$$

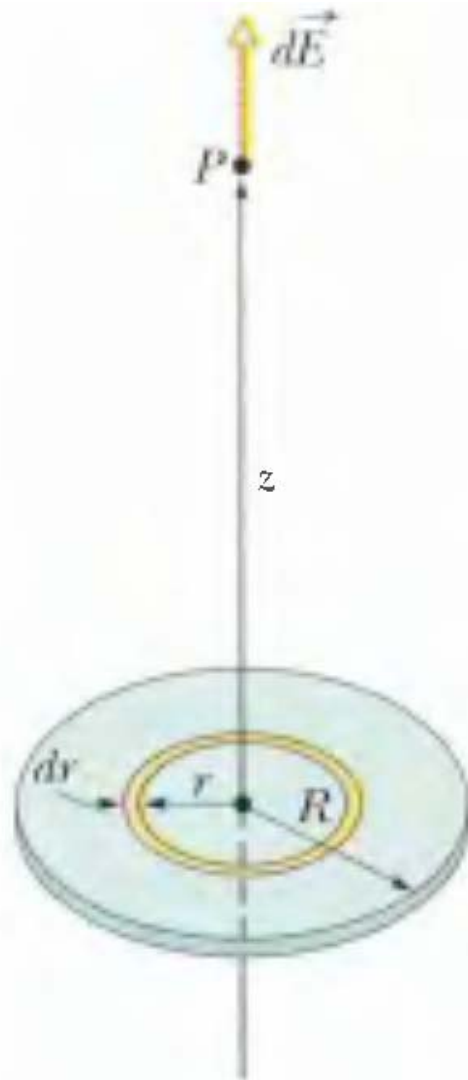


$$= \int dE \cos \theta = \frac{z \lambda}{4 \pi \epsilon_0 (z^2 + R^2)^{3/2}} \int_0^{2\pi R} ds$$

$$= \frac{z \lambda (2 \pi R)}{4 \pi \epsilon_0 (z^2 + R^2)^{3/2}}$$



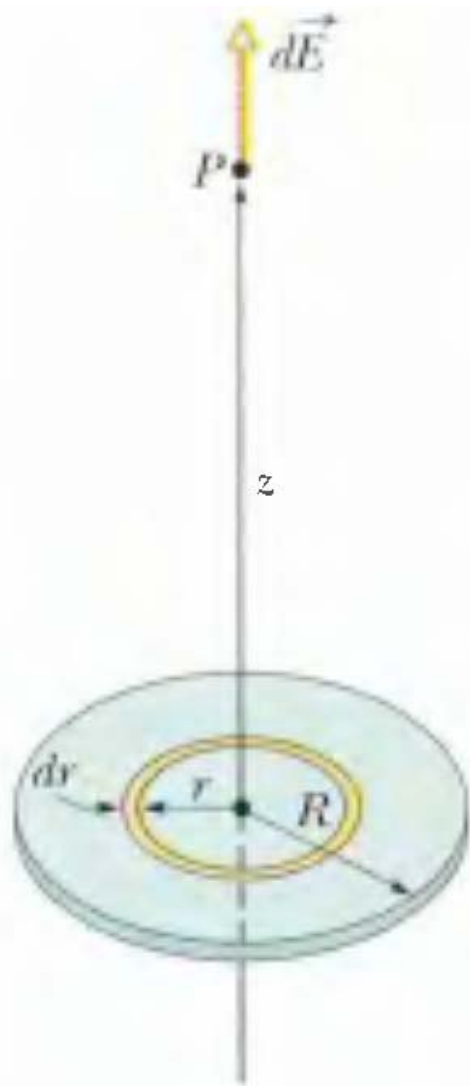
$$E = \frac{qz}{4\pi\epsilon_0(z^2 + R^2)^{3/2}} \quad (\text{charged ring})$$



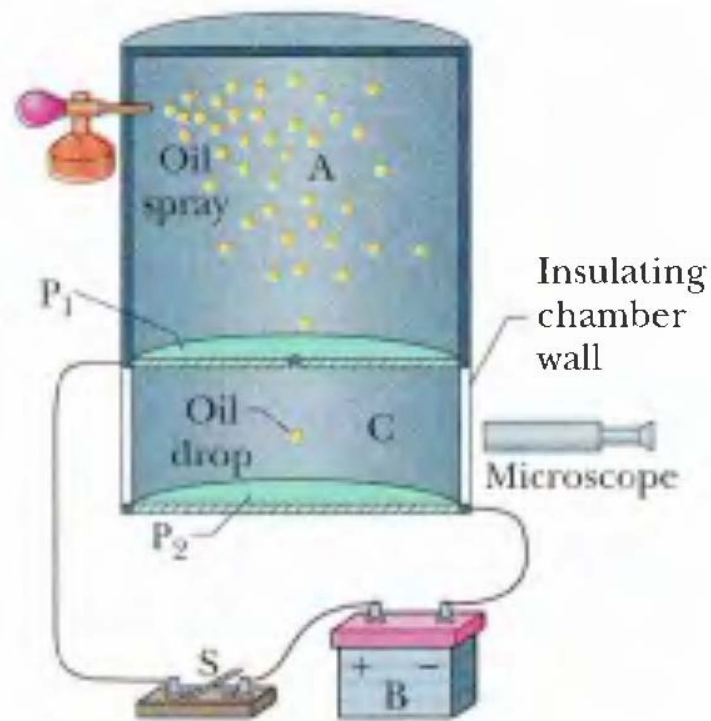
$$dq = \sigma dA = \sigma (2\pi r dr),$$

$$dE = \frac{z\sigma 2\pi r dr}{4\pi\epsilon_0(z^2 + r^2)^{3/2}},$$

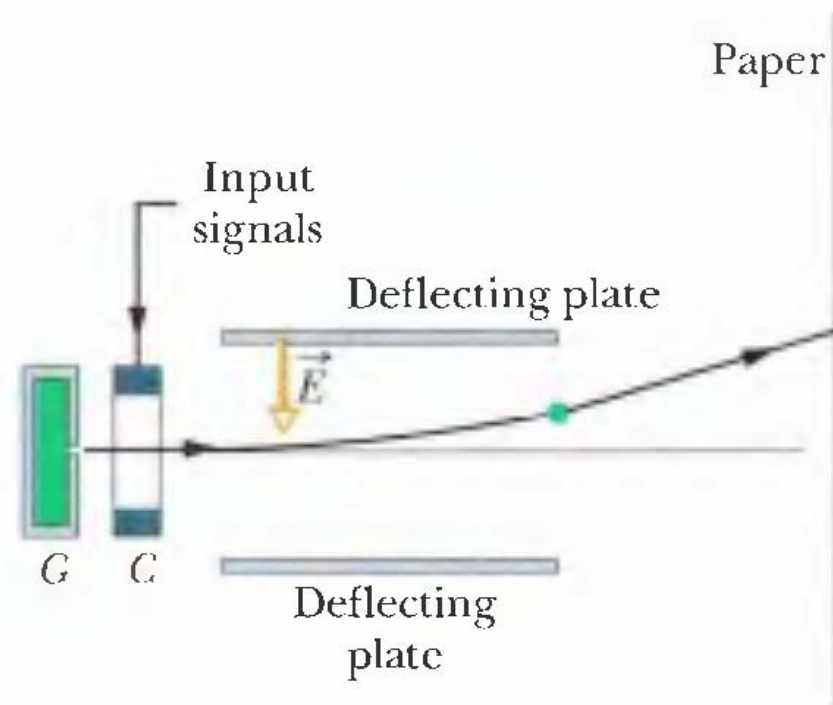
$$dE = \frac{\sigma z}{4\epsilon_0} \frac{2r dr}{(z^2 + r^2)^{3/2}}.$$



$$E = \frac{\sigma}{2\epsilon_0} \left( 1 - \frac{z}{\sqrt{z^2 + R^2}} \right) \quad \text{(charged disk)}$$

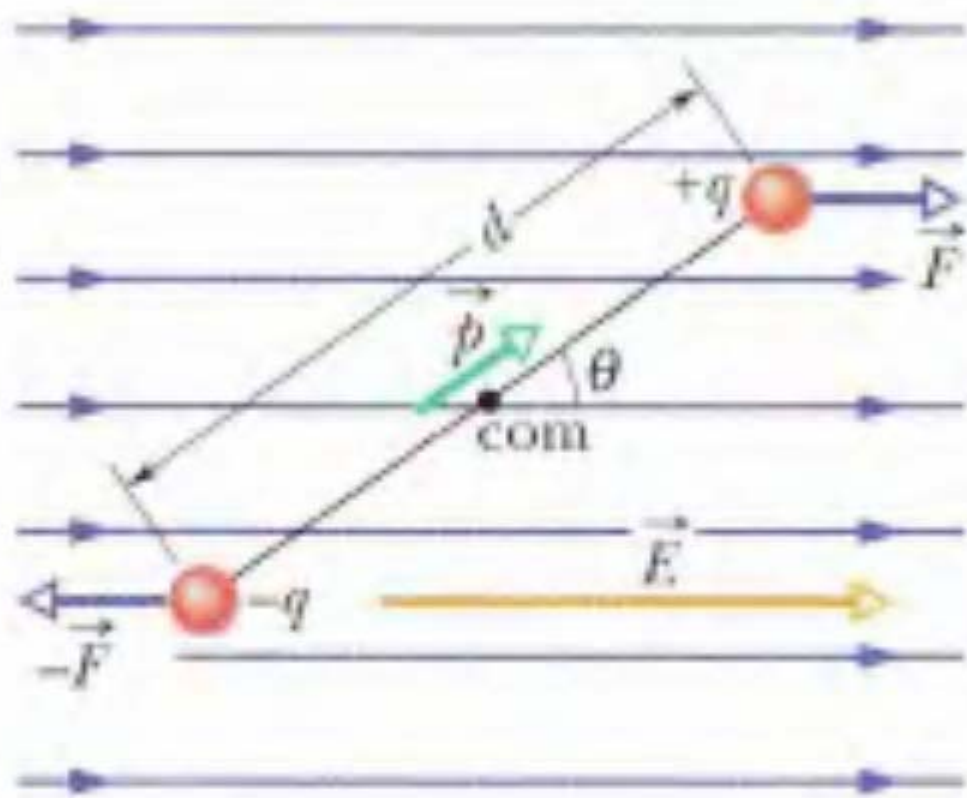


**FIG. 22-14** The Millikan oil-drop apparatus for measuring the elementary charge  $e$ . When a charged oil drop drifted into chamber C through the hole in plate  $P_1$ , its motion could be controlled by closing and opening switch S and thereby setting up or eliminating an electric field in chamber C. The microscope was used to view the drop, to permit timing of its motion.



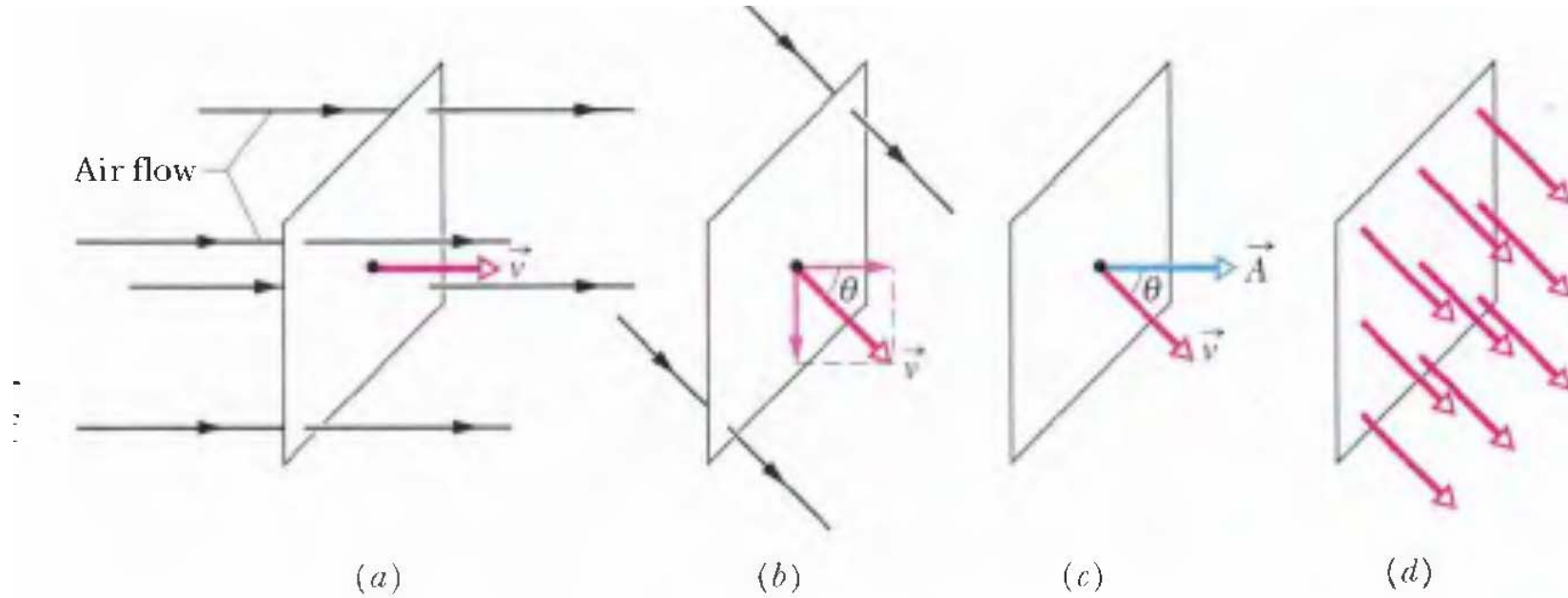
**FIG. 22-15** The essential features of an ink-jet printer. Drops are shot out from generator  $G$  and receive a charge in charging unit  $C$ . An input signal from a computer controls the charge given to each drop and thus the effect of field  $\vec{E}$  on the drop and the position on the paper at which the drop lands. About 100 tiny drops are needed to form a single character.





(a)

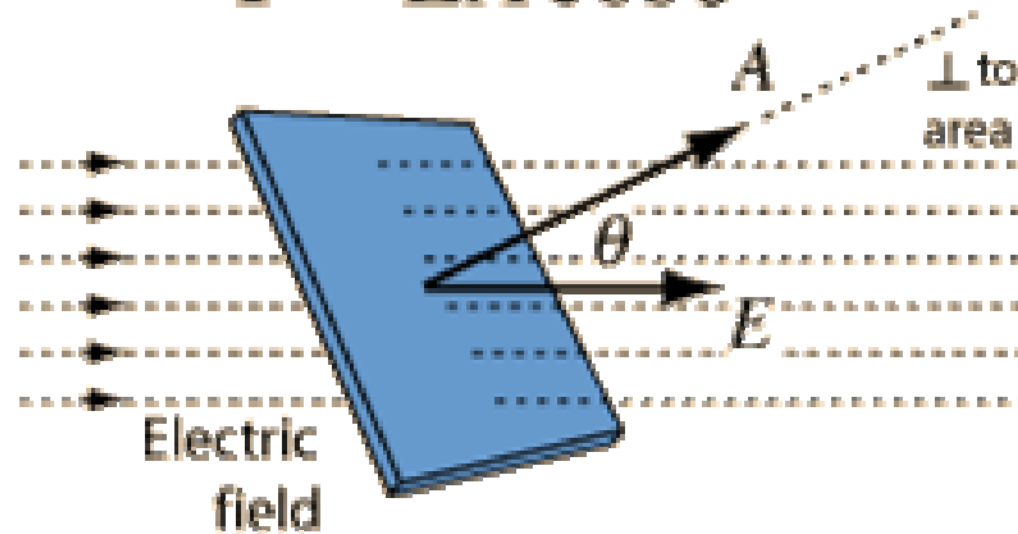
# flux

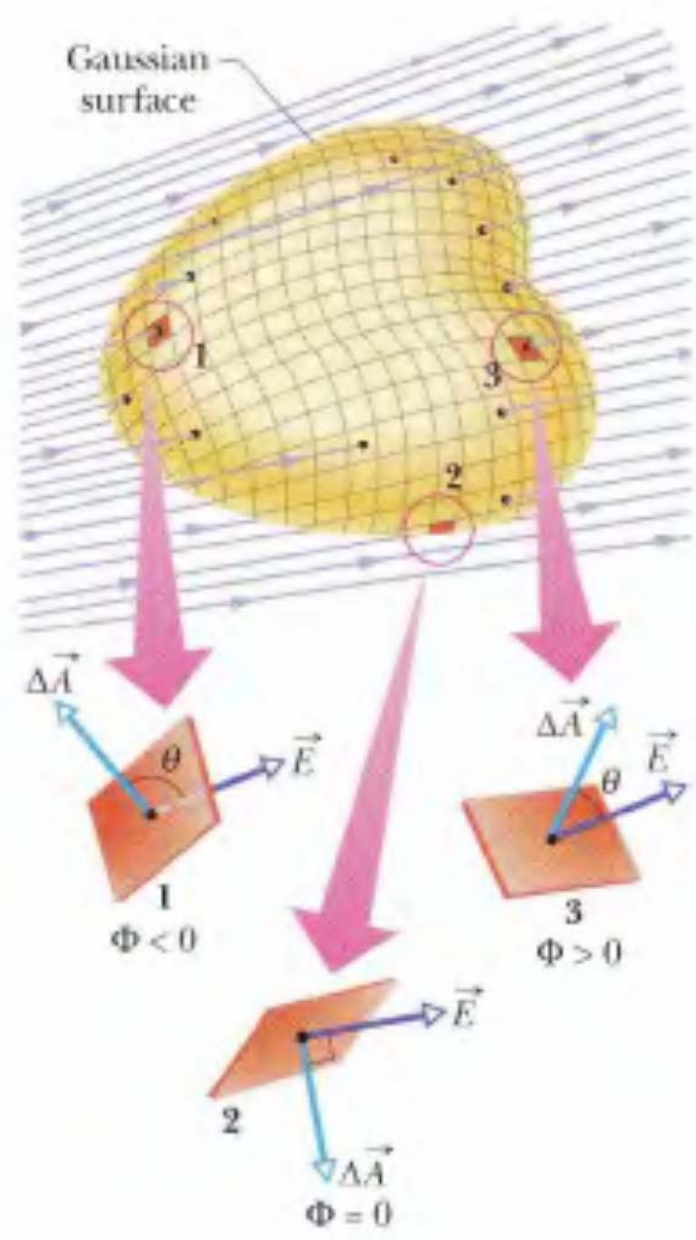


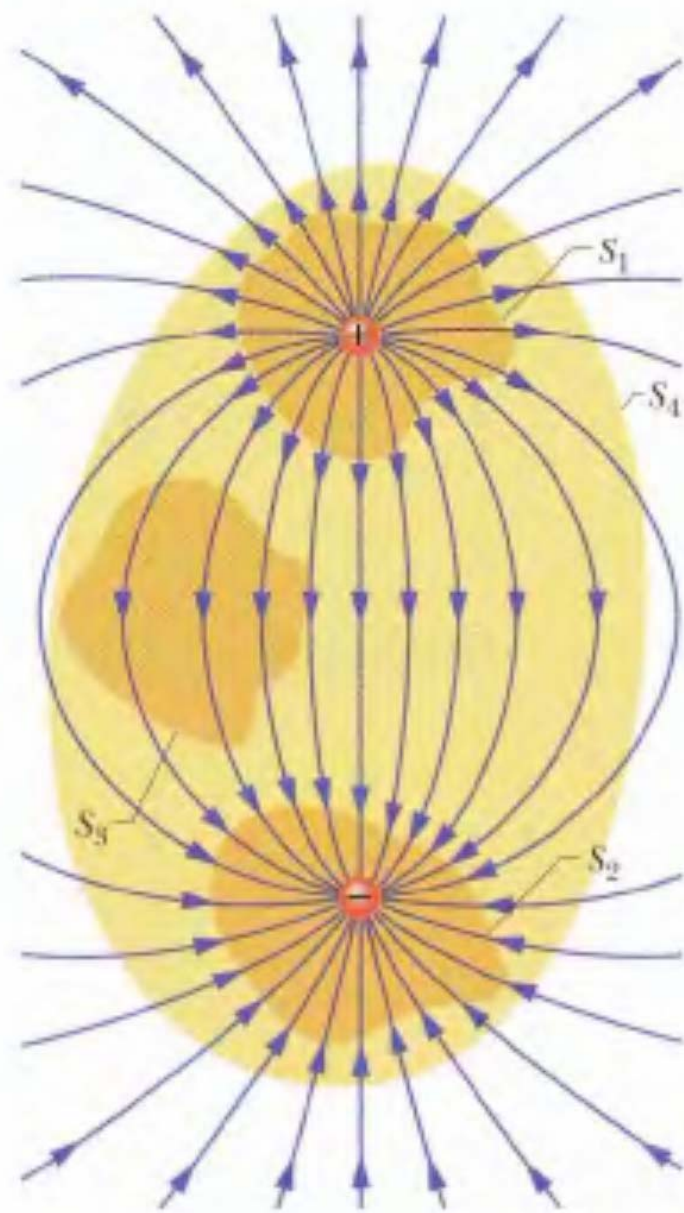
$$\Phi = vA \cos \theta = \vec{v} \cdot \vec{A},$$

# electric flux

$$\text{flux} = \Phi = EA \cos \theta$$







The total of the electric flux out of a closed surface is equal to the charge enclosed divided by the permittivity.

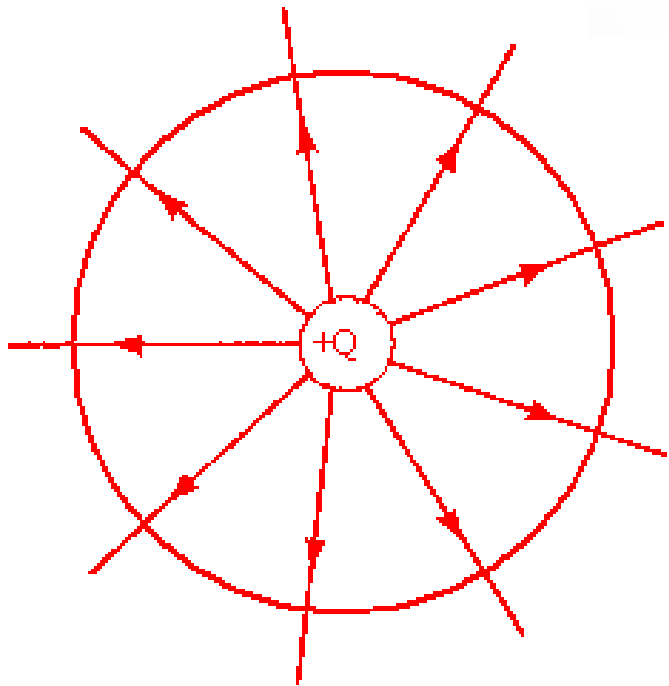
$$\Phi = \oint \vec{E} \cdot d\vec{A} \quad (\text{electric flux through a Gaussian surface}).$$

$$\epsilon_0 \Phi = q_{\text{enc}} \quad (\text{Gauss' law}).$$

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = q_{\text{enc}} \quad (\text{Gauss' law}).$$

# Gauss' Law and Coulomb's Law

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = \epsilon_0 \oint E dA = q_{\text{enc.}}$$



$$\epsilon_0 E \oint dA = q.$$

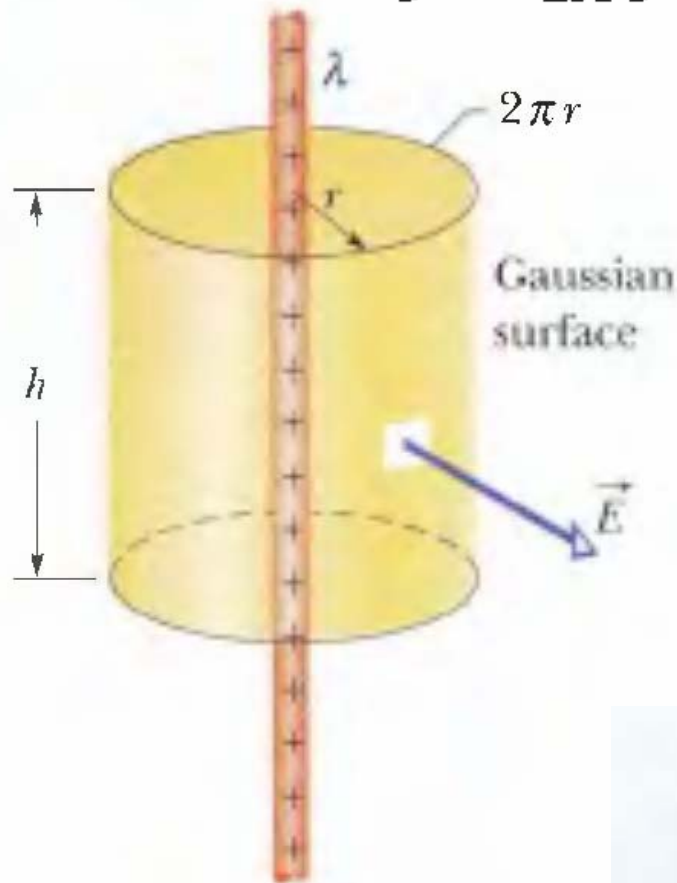
$$\epsilon_0 E (4\pi r^2) = q$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}.$$



## Applying Gauss' Law: Cylindrical Symmetry

$$\Phi = EA \cos \theta = E(2\pi rh) \cos 0 = E(2\pi rh).$$



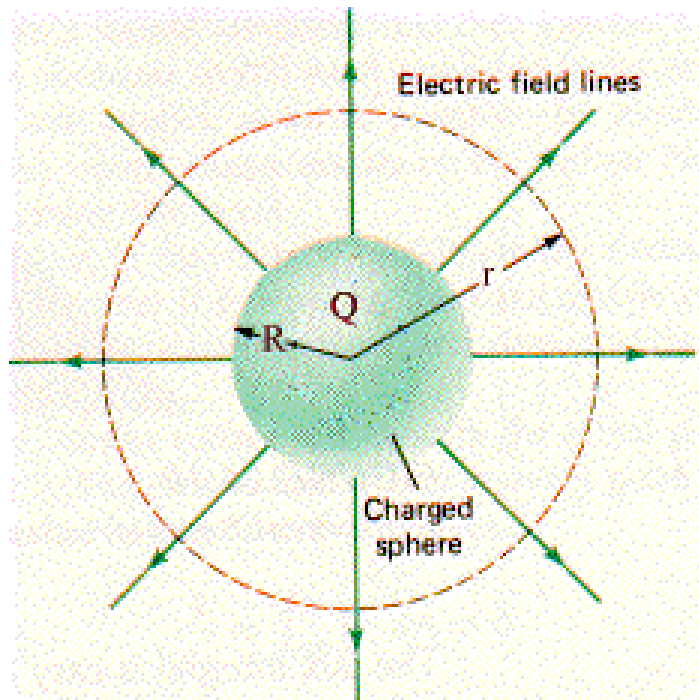
$$\epsilon_0 \Phi = q_{\text{enc}},$$

$$\epsilon_0 E(2\pi rh) = \lambda h,$$

$$E = \frac{\lambda}{2\pi\epsilon_0 r} \quad (\text{line of charge}).$$

## Electric field for a uniform sphere of charge

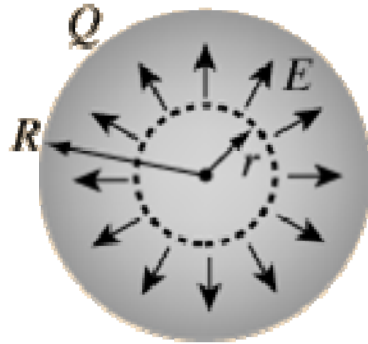
$r > R$



$$\Phi = EA = E4\pi r^2 = \frac{Q}{\epsilon_0}$$

For  $r > R$

$$E = \frac{Q}{4\pi\epsilon_0 r^2}$$



$$\frac{Q'}{Q} = \frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi R^3} \quad \text{or} \quad Q' = Q \frac{r^3}{R^3}$$

$$\Phi = E4\pi r^2 = \frac{Qr^3}{\epsilon_0 R^3}$$

$$E = \frac{Qr}{4\pi\epsilon_0 R^3}$$

